

Neutrino Masses: Synergies Between The Energy & Intensity Frontiers

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In the context of the Standard Model:

$$L_a = \begin{pmatrix} \nu_a \\ l_a \end{pmatrix}_L, \quad a = 1, 2, 3$$

The leading SM gauge invariant operator is at dim-5:^{*}

$$\frac{1}{\Lambda} (y_\nu LH)(y_\nu LH) + h.c. \quad \Rightarrow \quad \frac{y_\nu^2 v^2}{\Lambda} \bar{\nu}_L \nu_R^c.$$

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The See-saw spirit: [†]

If $m_\nu \sim 1$ eV, then $\Lambda \sim y_\nu^2$ (10^{14} GeV).

$$\Lambda \Rightarrow \begin{cases} 10^{14} \text{ GeV for } y_\nu \sim 1; \\ 100 \text{ GeV for } y_\nu \sim 10^{-6}. \end{cases}$$



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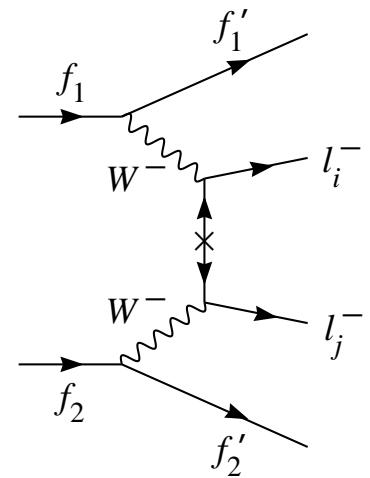
The See-saw implies the “synergy” !



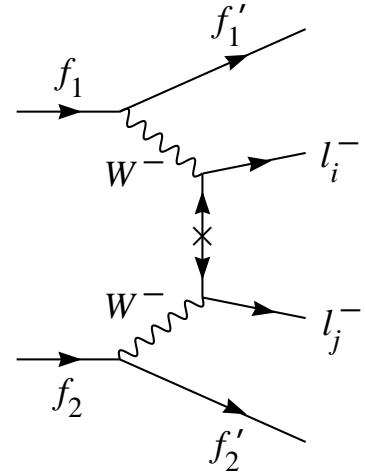
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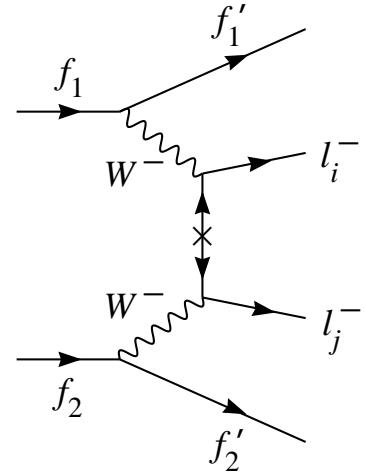


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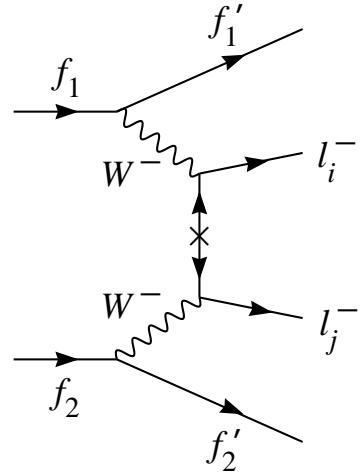
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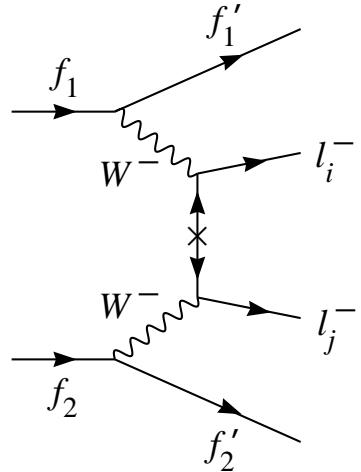
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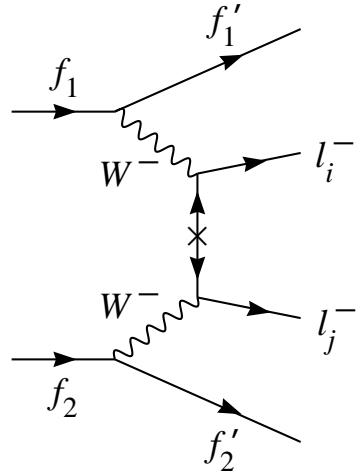
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Many theoretical models in SUSY, GUTs, SM extensions
(see talks by Mu-Chun Chen, Kayser, Pati, Babu, Mohapatra, Shafi ...)
We will stay in the minimal extension.

See-saw Models

Type I See-saw (with N_R):

$$L_{aL} = \begin{pmatrix} \nu_a \\ l_a \end{pmatrix}_L, \quad a = 1, 2, 3; \quad N_{bR}, \quad b = 1, 2, 3, \dots n \geq 2.$$

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N_R 's are “sterile”! No gauge interactions, only through mass mixing:

$$\sum_{a=1}^3 \sum_{b=1}^n \overline{\nu_{aL}} m_{ab}^\nu N_{bR} + \sum_{b,b'=1}^{n \geq 2} \overline{N^c}_{bL} M_{bb'} N_{b'R} + h.c.$$

$$(\overline{\nu_L} \quad \overline{N^c}_L) \begin{pmatrix} 0_{3 \times 3} & D_{3 \times n}^\nu \\ D_{n \times 3}^{\nu T} & M_{n \times n} \end{pmatrix} \begin{pmatrix} \nu^c_R \\ N_R \end{pmatrix}$$

All Majorana neutrinos:

$$\nu_{aL} = \sum_{m=1}^3 U_{am} \nu_{mL} + \sum_{m'=4}^{3+n} V_{am'} N_{m'L}^c,$$

$$N_{aL}^c = \sum_{m=1}^3 X_{am} \nu_{mL} + \sum_{m'=4}^{3+n} Y_{am'} N_{m'L}^c,$$

$$m_\nu \approx \frac{D^2}{M}, \quad m_N \approx M, \quad UU^\dagger \approx I \text{ (PMNS)}, \quad VV^\dagger \approx \frac{m_\nu}{m_N}.$$

The charged currents:

$$\begin{aligned}-\mathcal{L}_{CC} &= \frac{g}{\sqrt{2}} W_\mu^+ \sum_{\ell=e}^{\tau} \sum_{m=1}^3 U_{\ell m}^* \bar{\nu}_m \gamma^\mu P_L \ell + h.c. \\ &+ \frac{g}{\sqrt{2}} W_\mu^+ \sum_{\ell=e}^{\tau} \sum_{m'=4}^{3+n} V_{\ell m'}^* \bar{N}_{m'}^c \gamma^\mu P_L \ell + h.c.\end{aligned}$$

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Still, it's possible for much lower see-saw scales[†], and sizable mixing[‡].

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All $U_{\ell m}$, Δm_ν are from oscillation experiments,
while taking $V_{\ell m}$, m_N free parameters
— in the hope, experimentally accessible.

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Type II see-saw (no N_R): *

With a scalar triplet Φ ($Y = 2$) : $\phi^{\pm\pm}, \phi^\pm, \phi^0$ (many representative models).
Add a gauge invariant/renormalizable term:

$$Y_{ij} \overline{L}_i^c (i\sigma_2) \Phi L_j + h.c.$$

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That leads to the Majorana mass:

$$M_{ij} \overline{\nu}_i^c \nu_j + h.c. \quad \text{where} \quad M_{ij} = Y_{ij} \langle \Phi \rangle = Y_{ij} v' \lesssim 1 \text{ eV},$$

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Main feature(s):

Doubly charged Higgs and their $\Delta L = 2$ decay.

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Type III see-saw (no N_R , but some other leptons): *

With a lepton triplet T ($Y = 0$): $T^+ \ T^0 \ T^-$, add the terms:

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Demand that $M_T \lesssim 1$ TeV, $M_{ij} \lesssim 1$ eV,

Thus the Yukawa couplings:[†]

$$y_j \lesssim 10^{-6},$$

making the mixing $T^{\pm,0} - \ell^{\pm}$ very weak.

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Main features:

T^0 a Majorana neutrino;

Decay via mixing (Yukawa couplings);

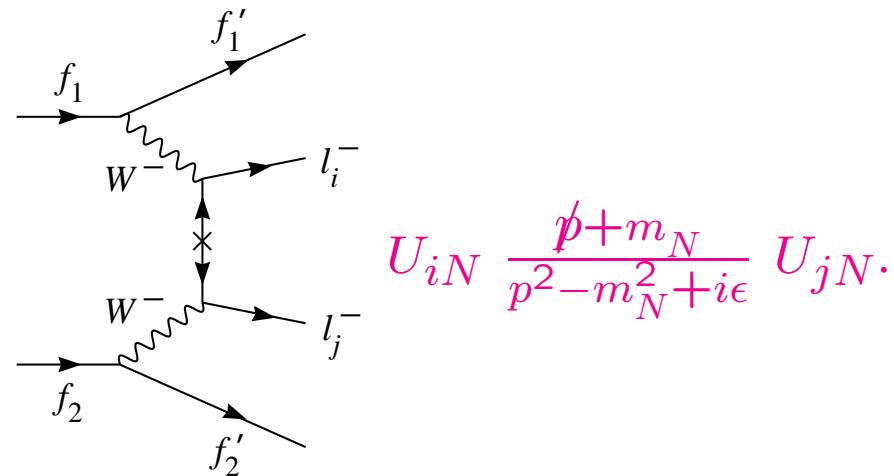
$T\bar{T}$ Pair production via EW gauge interactions.

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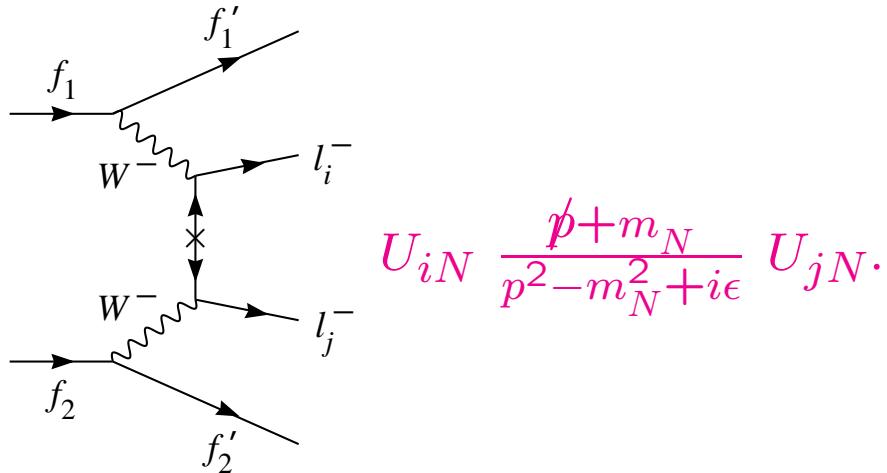
The Search for $\Delta L = 2$ Processes

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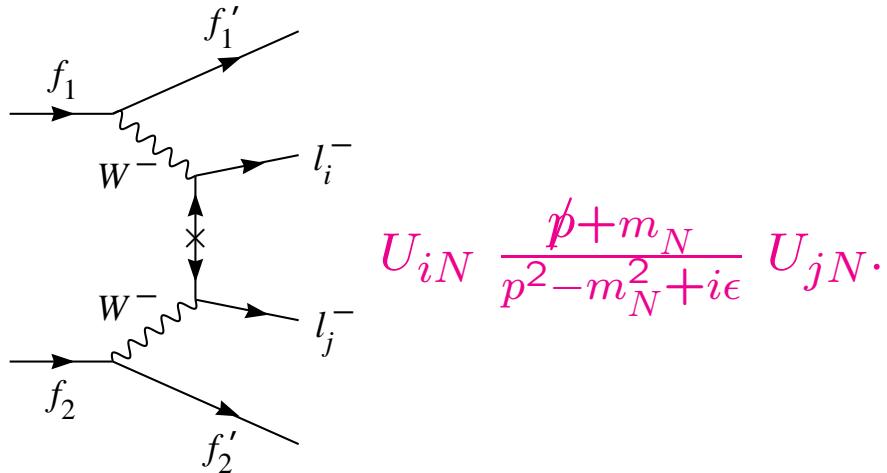


The transition rates are proportional to

$$|\mathcal{M}|^2 \propto \begin{cases} \langle m \rangle_{ee}^2 = \left| \sum_{i=1}^3 U_{ei} U_{ei} m_i \right|^2 & \text{for light } \nu \Rightarrow \langle m \rangle_{ee} \sim \mathcal{O}(0.1 \text{ eV}) \\ \frac{\left| \sum_i^n V_{ei} V_{ei} \right|^2}{m_N^2} & \text{for heavy } N \Rightarrow |V_{eN}|^2 / m_N < 5 \times 10^{-8} \text{ GeV}^{-1} \end{cases}$$

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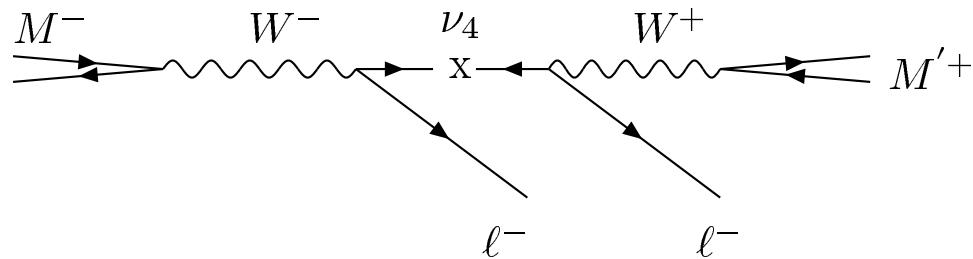


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This afternoon session.

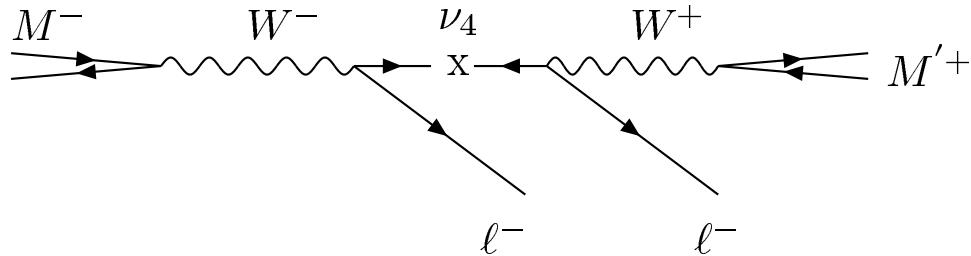
(2). N Resonance Production and Decay



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We calculated[†] all the τ , K , D , B decays: $M^+ \rightarrow \ell_i^+ \ell_j^+ M^-$ via N and compare with the existing experimental bounds.*

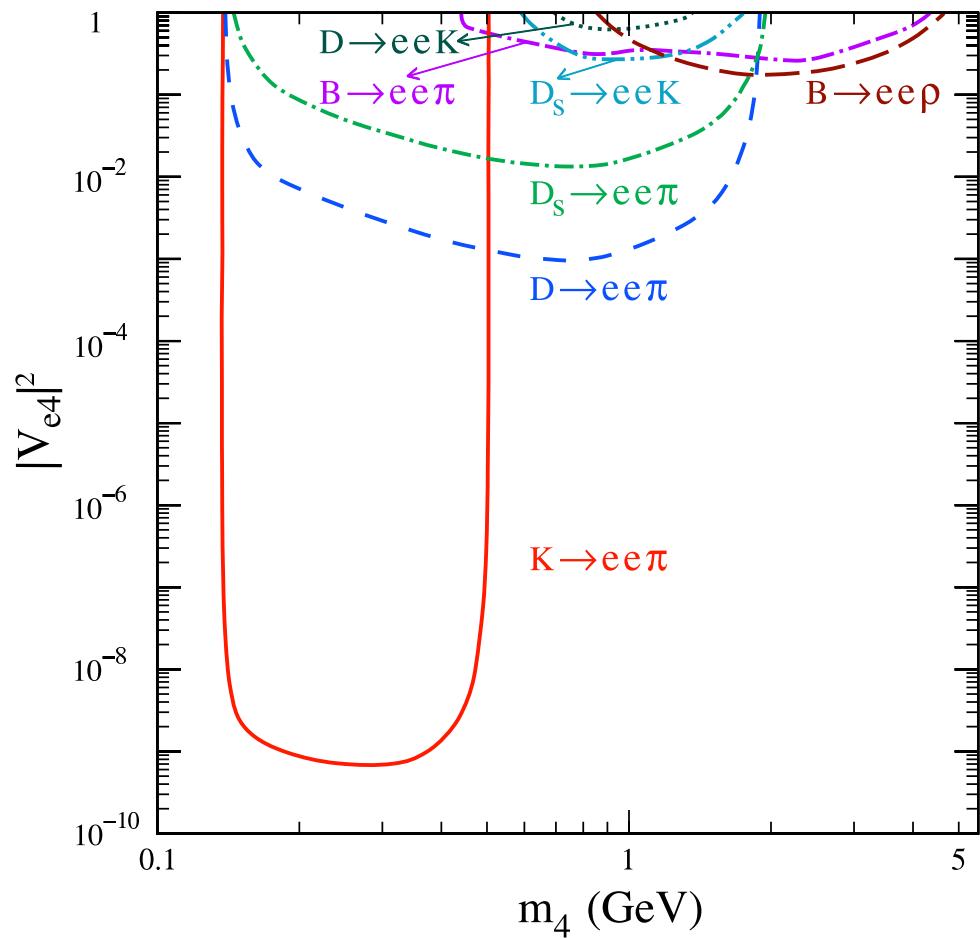
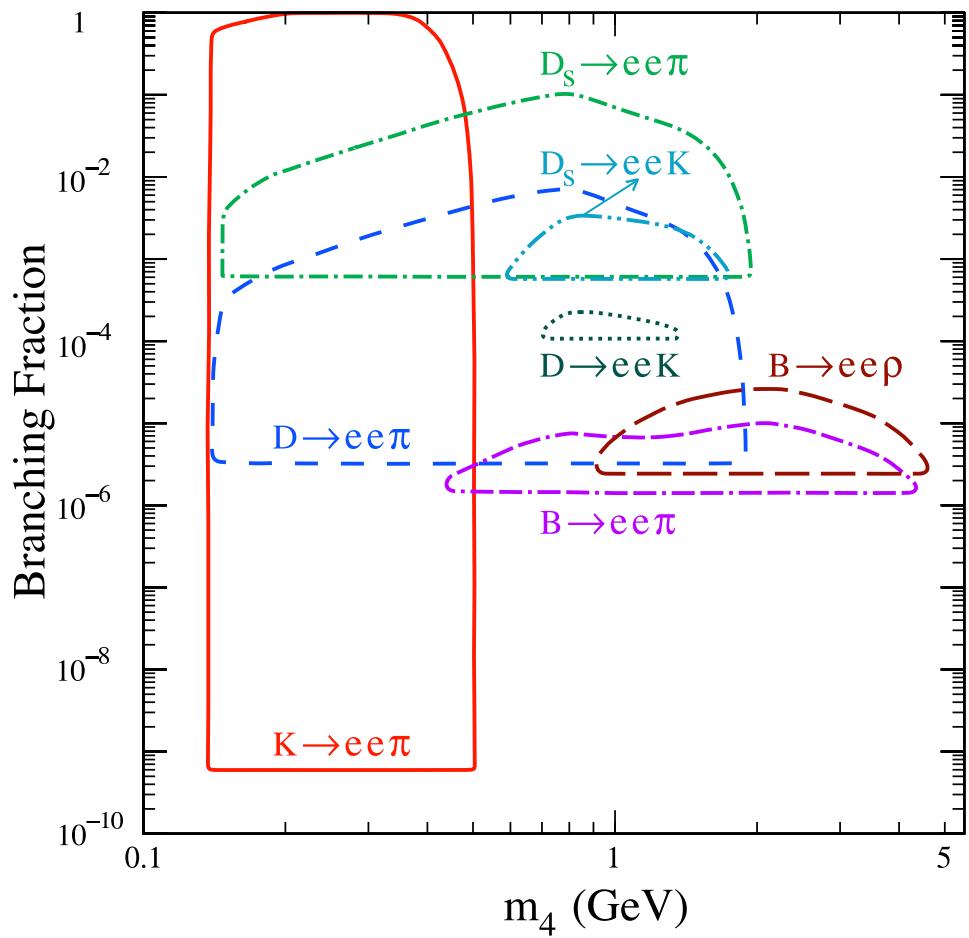
We scan the parameters in the range:

$$\begin{aligned} 10^{-10} < |V_{e4}|^2, |V_{\mu 4}|^2, |V_{\tau 4}|^2 &< 0.2 \\ m_4 > 140 \text{ MeV}, m_e + m_\pi &\text{ threshold;} \\ \dots \dots \\ m_4 > 3.8 \text{ GeV}, m_\tau + M_D &\text{ threshold;} \\ m_4 \sim 5.2 \text{ GeV}, M_B &\text{ kinematics.} \end{aligned}$$

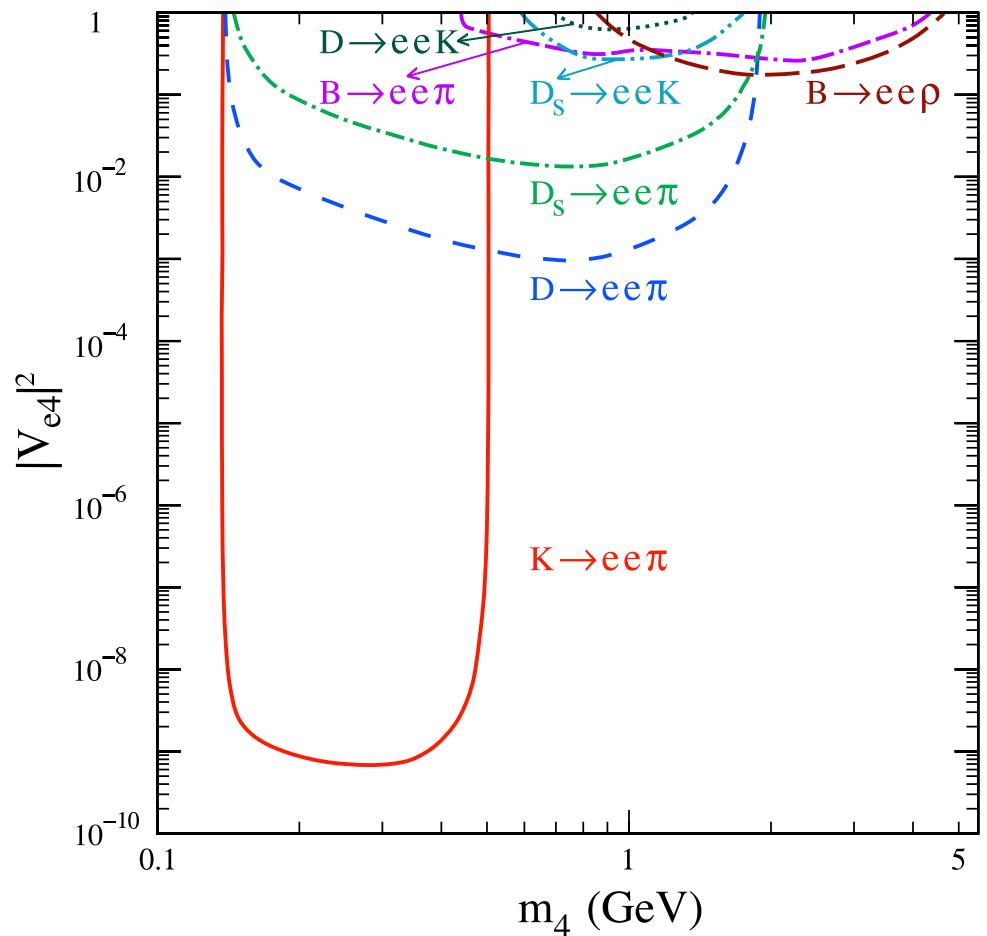
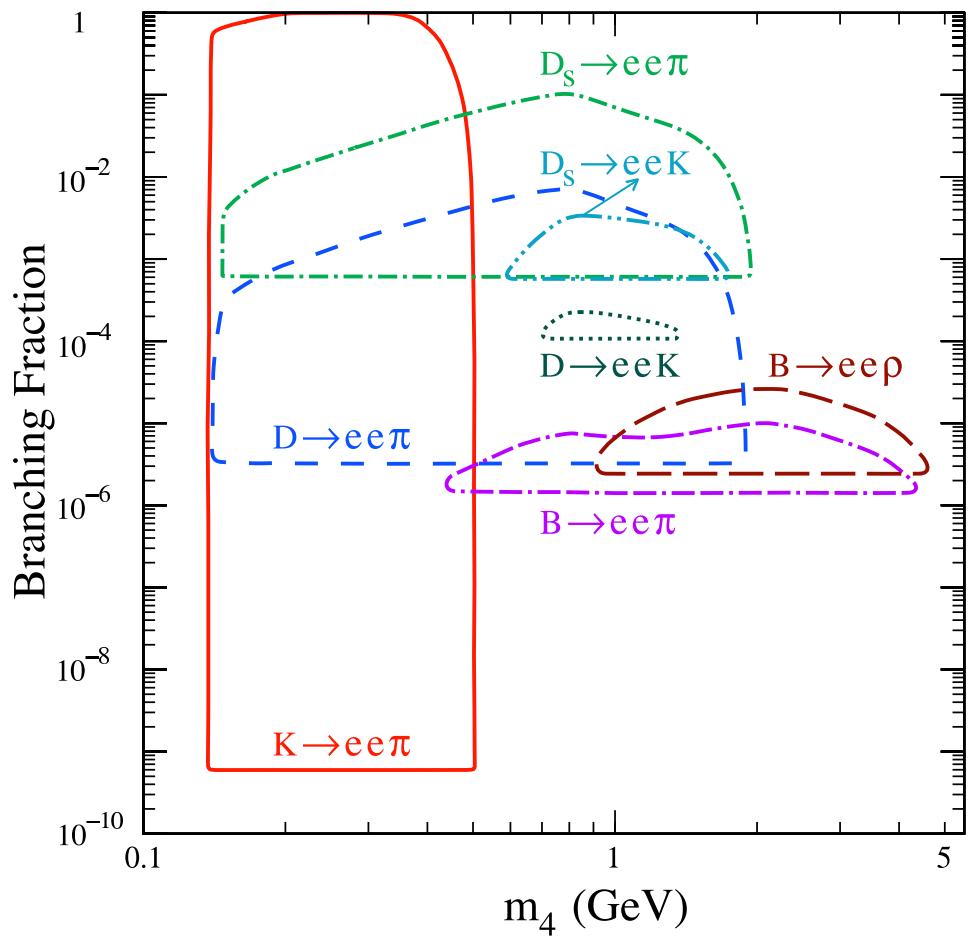
[†]A. Atre, T. Han, S. Pascoli, B. Zhang, arXiv.0901.3589.

*PDG.

Sensitivity to V_{e4} :

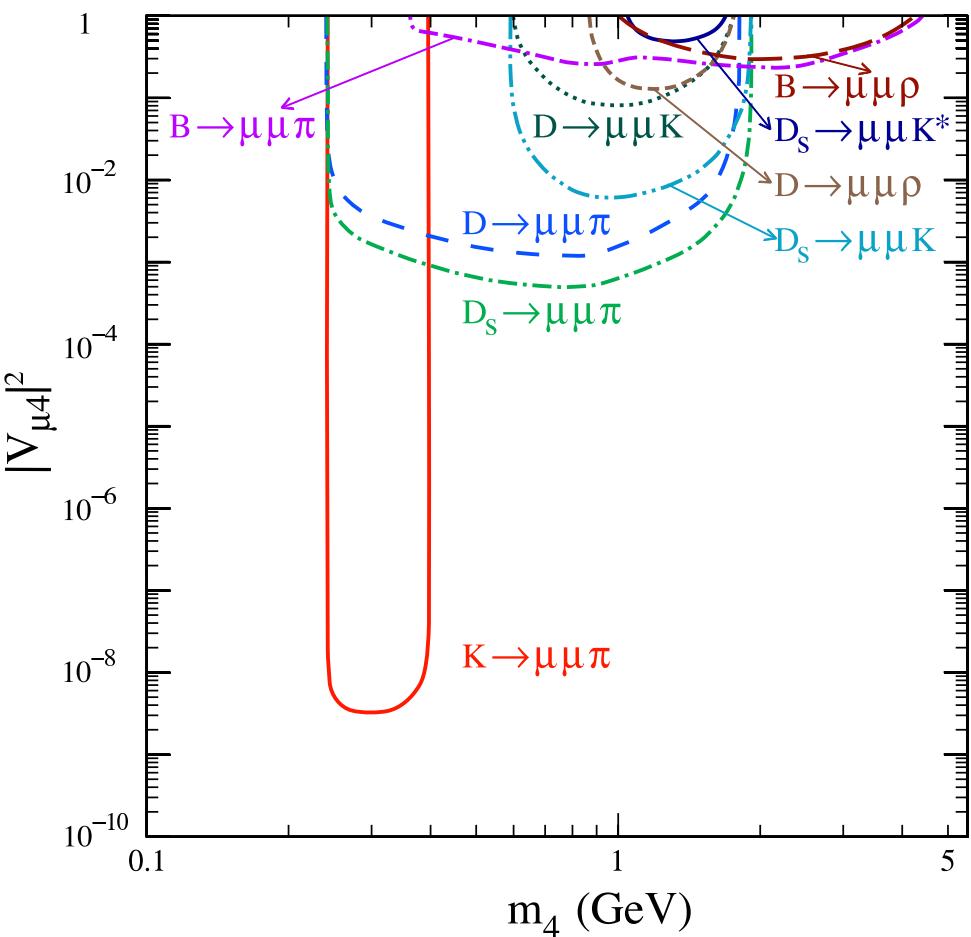
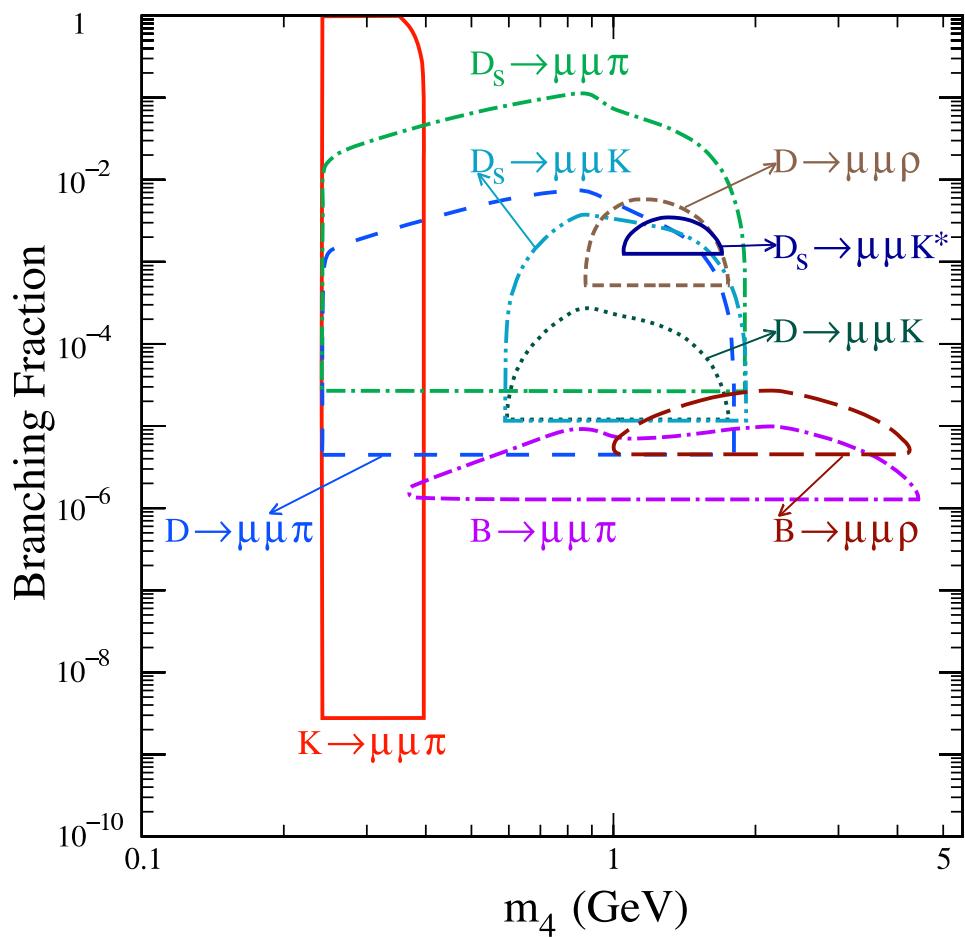


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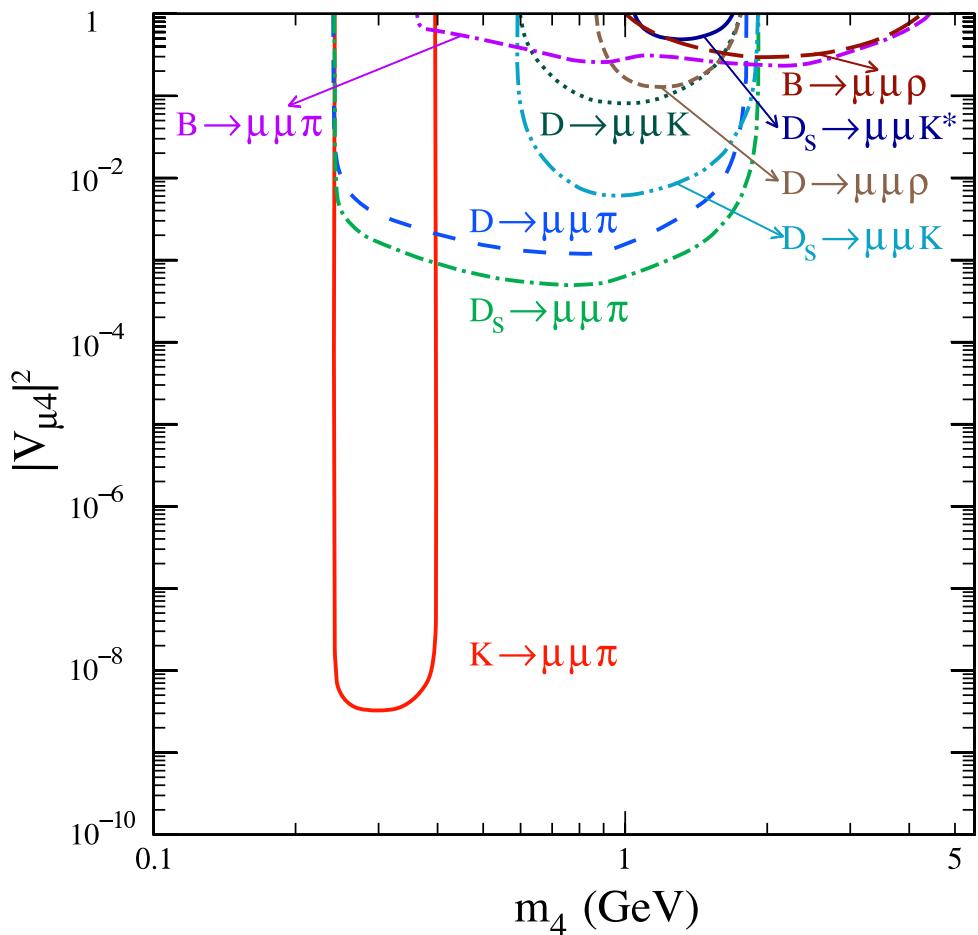
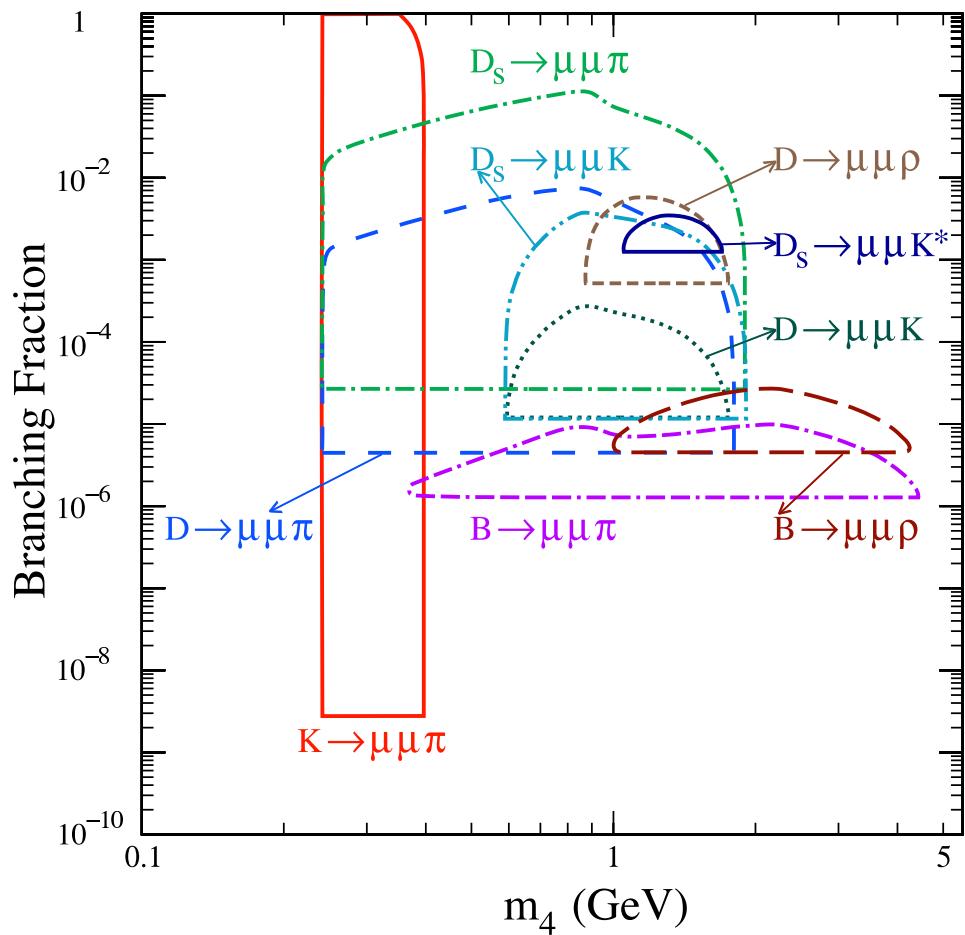


- Depending on the unknown parameter $|V_{e4}|^2$,
BR's can easily reach $10^{-6} - 10^{-2}$,
 N_4 may show up in any one of the channels !

Sensitivity to $V_{\mu 4}$:



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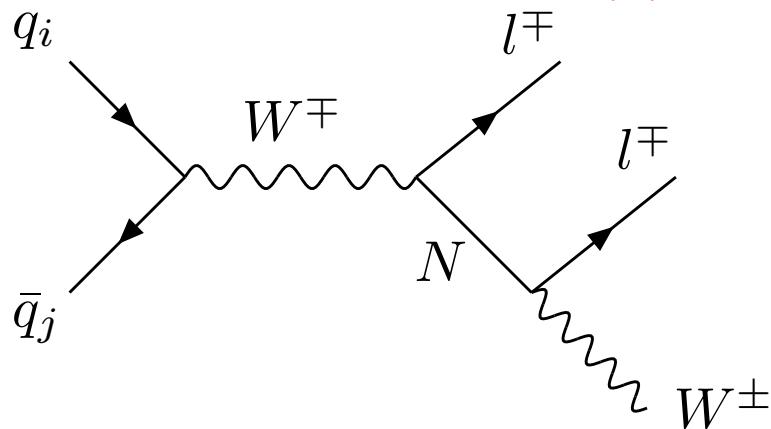


- Other processes to look for:

$D^+, B^+ \rightarrow \ell^+ \ell^+ K^*$,
 $B^+ \rightarrow \tau^+ e^+ M^-$, $\tau^+ \mu^+ M^-$, $\tau^+ \tau^+ M^-$.

(3). Collider searches for Majorana N

At hadron colliders: $\ddagger \quad pp(\bar{p}) \rightarrow \ell^\pm \ell^\pm jjX$

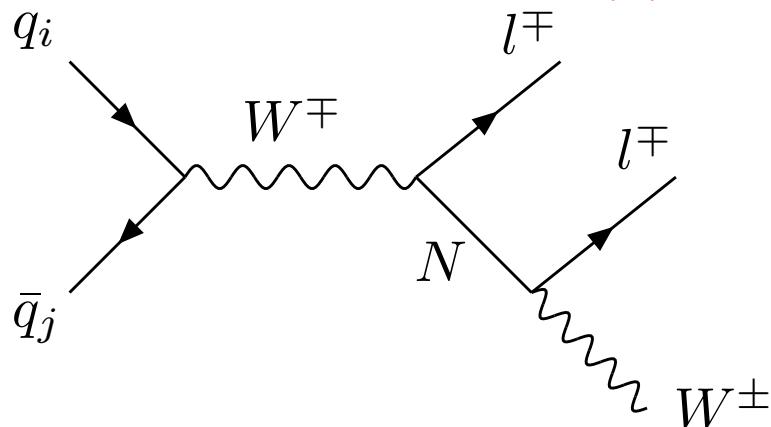


$$\sigma(pp \rightarrow \mu^\pm \mu^\pm W^\mp) \approx \sigma(pp \rightarrow \mu^\pm N) Br(N \rightarrow \mu^\pm W^\mp) \equiv \frac{V_{\mu N}^2}{\sum_l |V^{\ell N}|^2} V_{\mu N}^2 \sigma_0.$$

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Factorize out the mixing couplings: [†]

$$\sigma(pp \rightarrow \mu^\pm \mu^\pm W^\mp) \equiv S_{\mu\mu} \sigma_0,$$

$$S_{\mu\mu} = \frac{V_{\mu N}^4}{\sum_l |V_{\ell N}|^2} \approx \frac{V_{\mu N}^2}{1 + V_{\tau N}^2/V_{\mu N}^2}.$$

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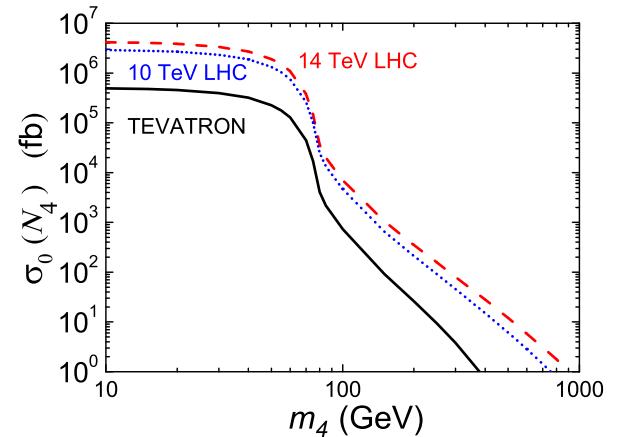
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- like-sign di-muons plus two jets;
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- $m(jj) = M_W$, $m(jj\mu) = m_N$.

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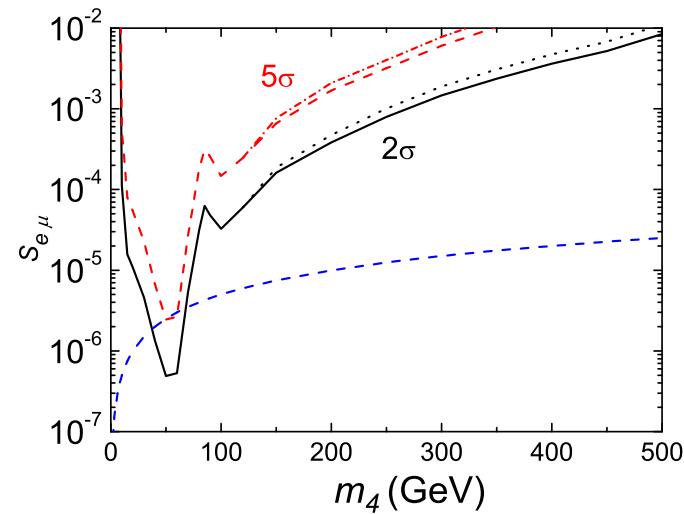
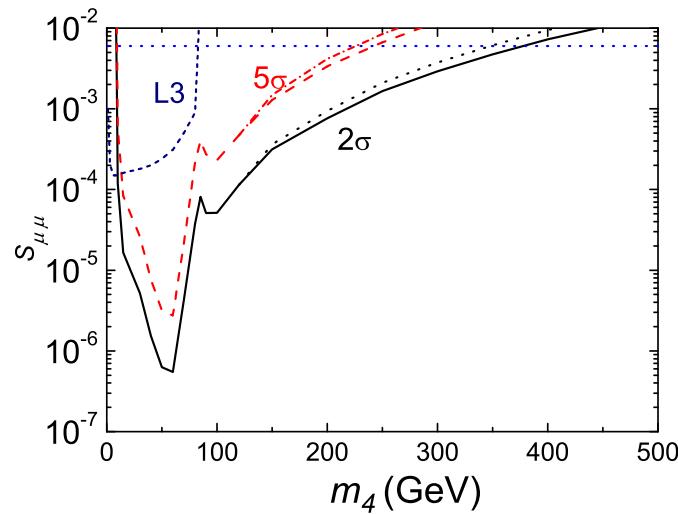


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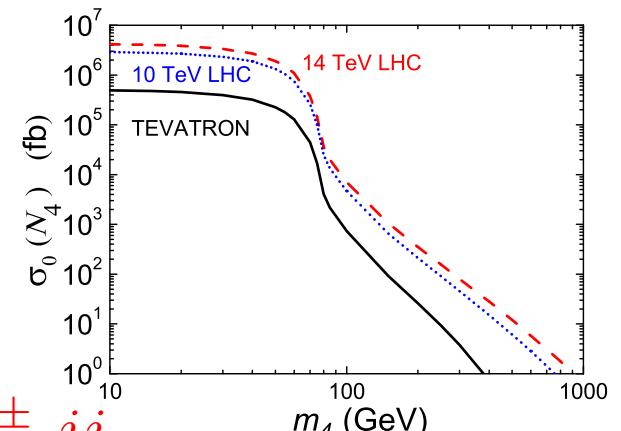
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- like-sign di-muons plus two jets;
- no missing energies;
- $m(jj) = M_W$, $m(jj\mu) = m_N$.

At the LHC:[†] $\mu^\pm \mu^\pm jj$ and $\mu^\pm e^\pm jj$



[†]A. Atre, T. Han, S. Pascoli, B. Zhang, arXiv.0901.3589.

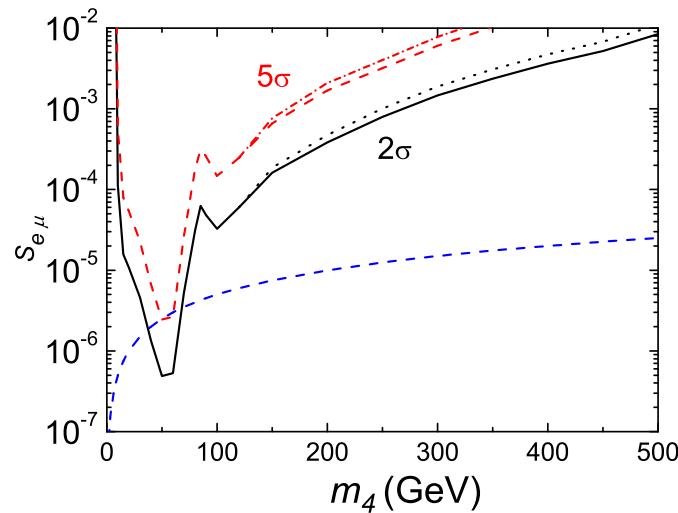
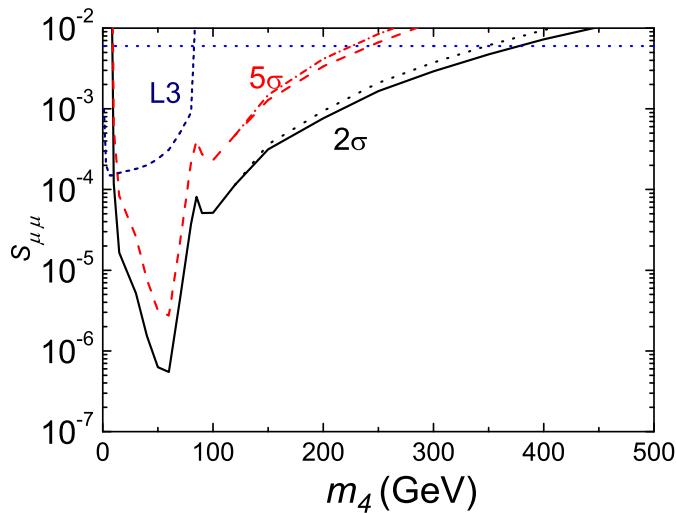
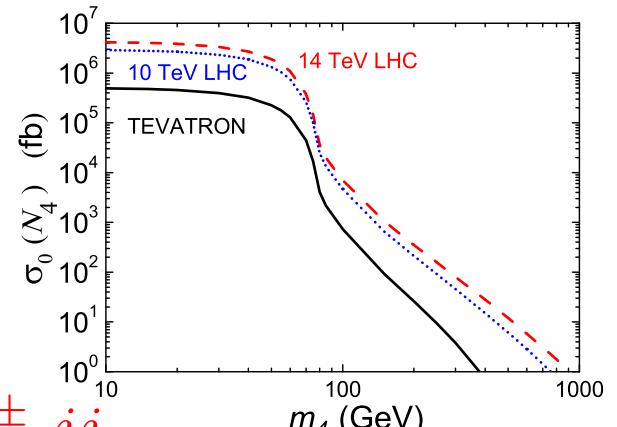


Consider $p\bar{p}$ (pp) $\rightarrow \mu^\pm \mu^\pm W^\mp \rightarrow \mu^\pm \mu^\pm jj$.

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Sensitivity reach:

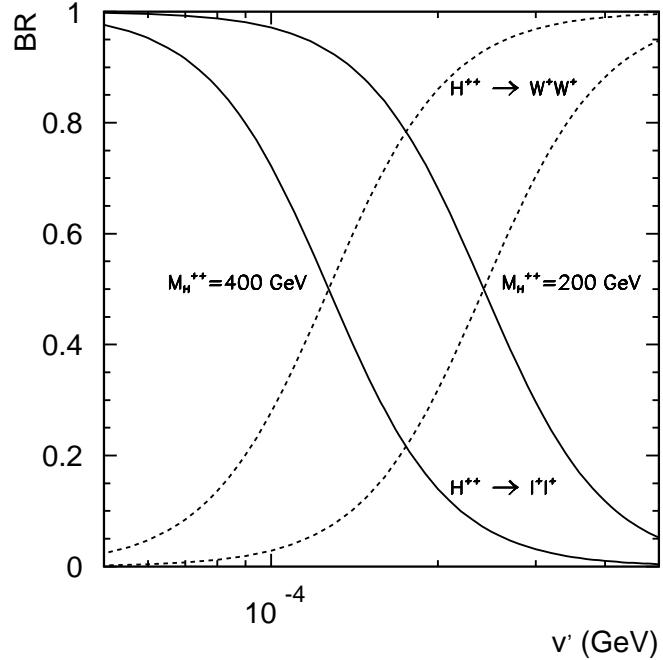
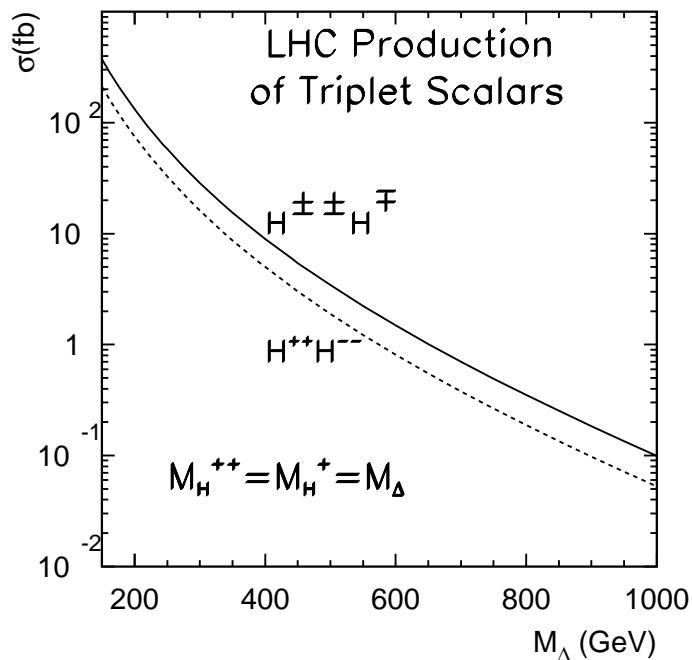
$\mu\mu$ mode: $V_{\mu\mu}^2 \sim 5 \times 10^{-7}$, or $m_4 \sim 400$ GeV.

$e\mu$ mode: $V_{e\mu}^2$ below $0\nu\beta\beta$ bound at $m_4 \sim M_W$.

[†]A. Atre, T. Han, S. Pascoli, B. Zhang, arXiv.0901.3589.

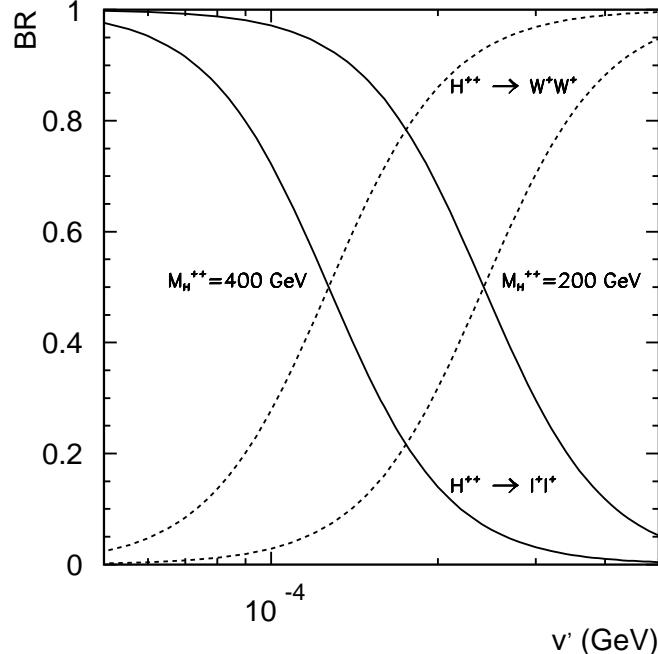
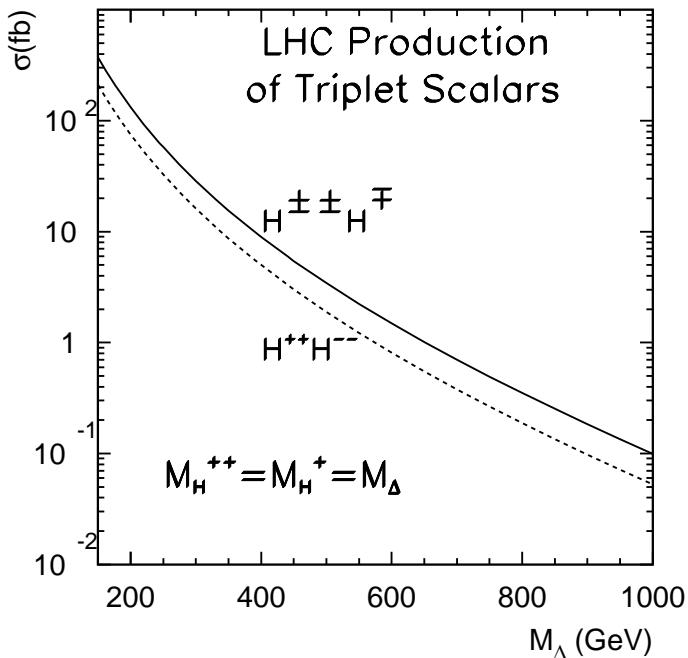
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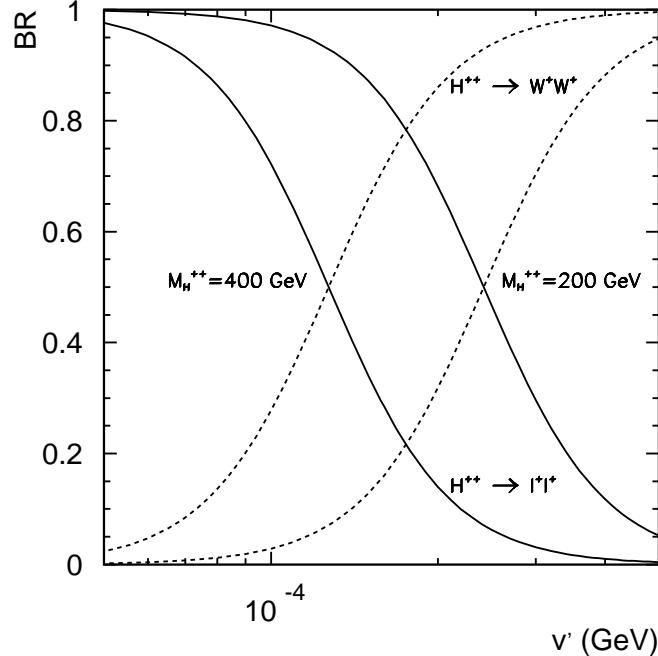
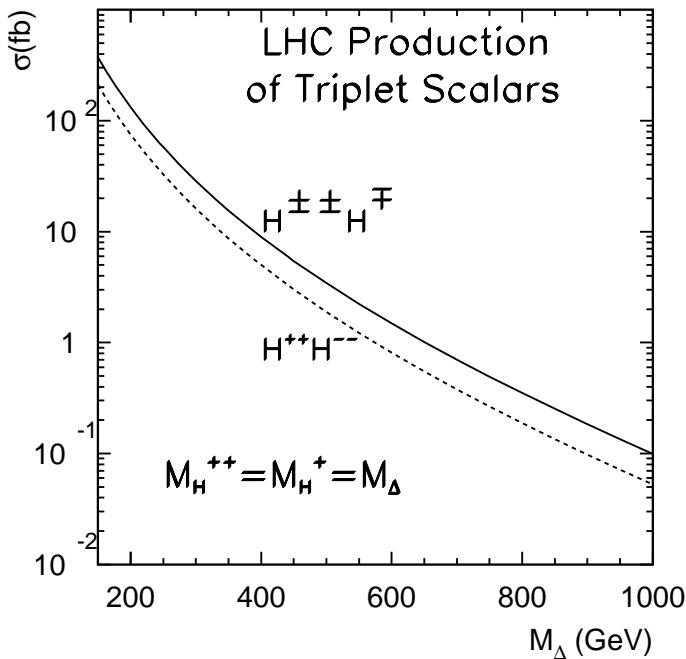
Unique decays:

$$\Gamma(\phi^{++} \rightarrow \ell^+\ell^+) \propto Y_{ij}^2 M_\phi, \quad \Gamma(\phi^{++} \rightarrow W^+W^+) \propto \frac{v'^2 M_\phi^3}{v^4},$$

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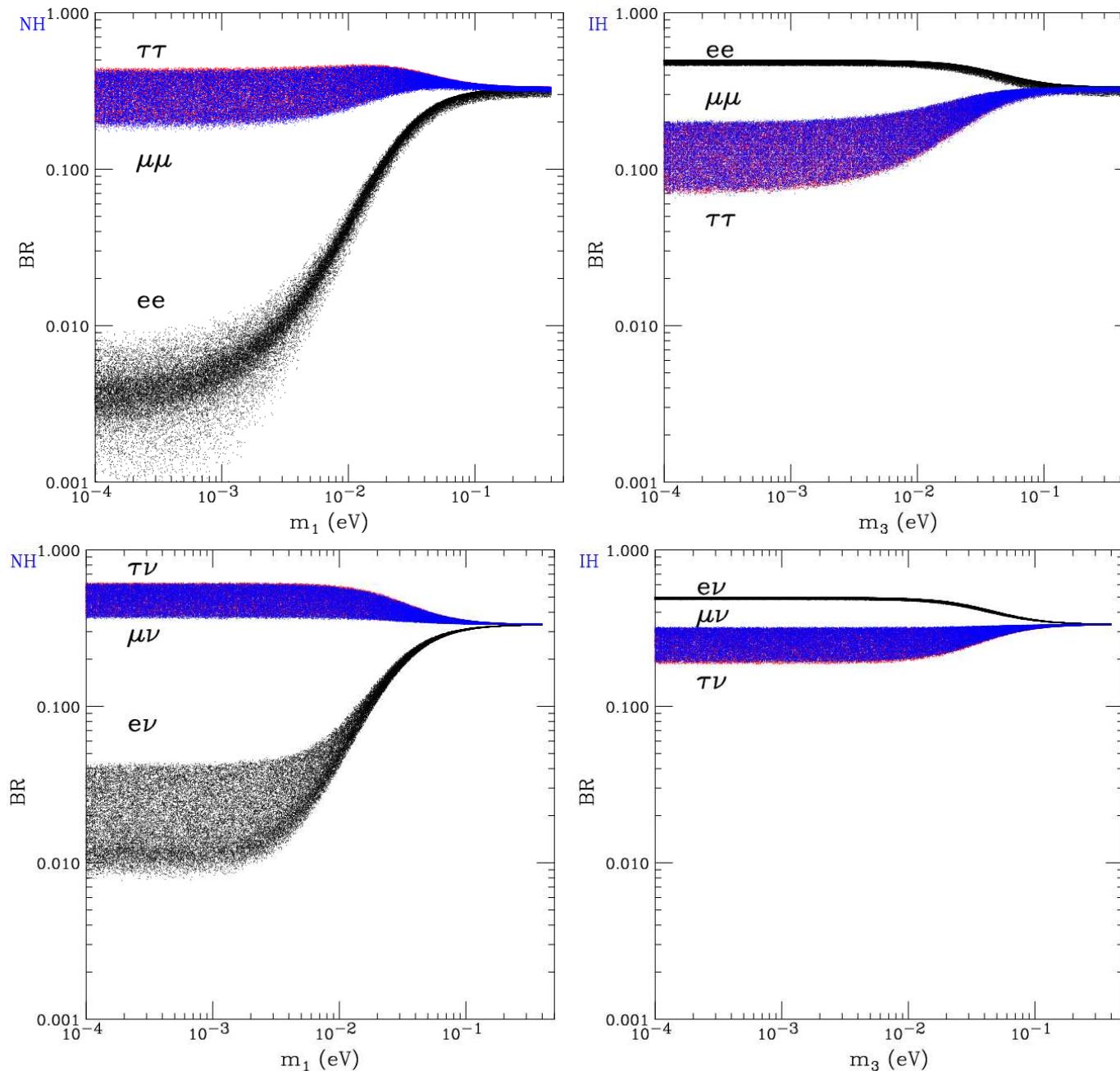
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Will concentrate on the leptonic modes. [†]

[†]Pavel Fileviez Perez, Tao Han, Gui-Yu Huang, Tong Li, Kai Wang,
arXiv:0803.3450 [hep-ph]

$H^{\pm\pm}, H^\pm$ decays predicted by the light neutrino spectrum:

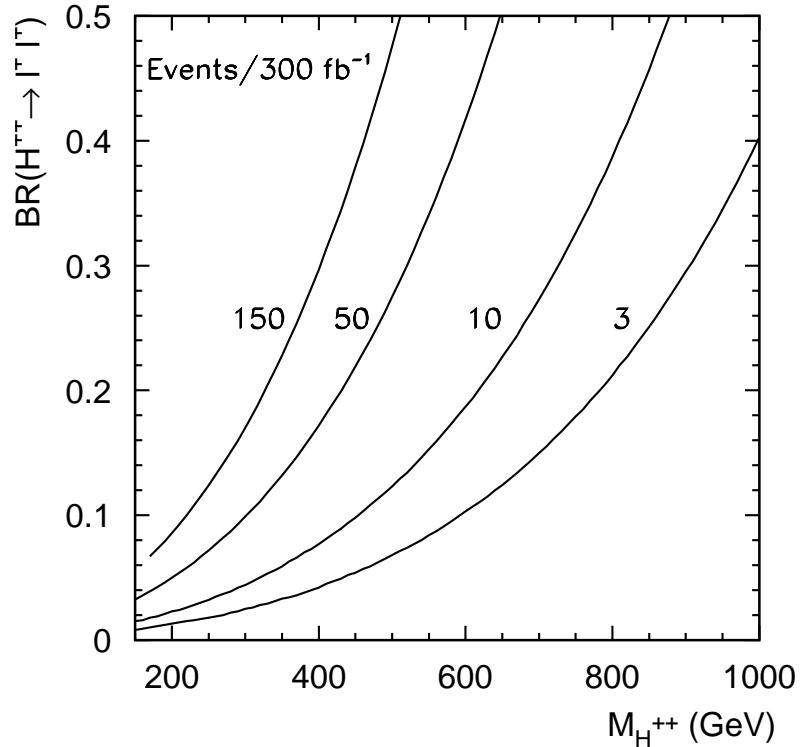


Summarize the discovery modes:

Spectrum	Relations
Normal Hierarchy $(\Delta m_{31}^2 > 0)$	$\text{BR}(H^{++} \rightarrow \tau^+ \tau^+), \text{BR}(H^{++} \rightarrow \mu^+ \mu^+) \gg \text{BR}(H^{++} \rightarrow e^+ e^+)$ $\text{BR}(H^{++} \rightarrow \mu^+ \tau^+) \gg \text{BR}(H^{++} \rightarrow e^+ \mu^+), \text{BR}(H^{++} \rightarrow e^+ \tau^+)$ $\text{BR}(H^+ \rightarrow \tau^+ \bar{\nu}), \text{BR}(H^+ \rightarrow \mu^+ \bar{\nu}) \gg \text{BR}(H^+ \rightarrow e^+ \bar{\nu})$
Inverted Hierarchy $(\Delta m_{31}^2 < 0)$	$\text{BR}(H^{++} \rightarrow e^+ e^+) > \text{BR}(H^{++} \rightarrow \mu^+ \mu^+), \text{BR}(H^{++} \rightarrow \tau^+ \tau^+)$ $\text{BR}(H^{++} \rightarrow \mu^+ \tau^+) \gg \text{BR}(H^{++} \rightarrow e^+ \tau^+), \text{BR}(H^{++} \rightarrow e^+ \mu^+)$ $\text{BR}(H^+ \rightarrow e^+ \bar{\nu}) > \text{BR}(H^+ \rightarrow \mu^+ \bar{\nu}), \text{BR}(H^+ \rightarrow \tau^+ \bar{\nu})$
Quasi-Degenerate $(m_1, m_2, m_3 > \Delta m_{31})$	$\text{BR}(H^{++} \rightarrow e^+ e^+) \sim \text{BR}(H^{++} \rightarrow \mu^+ \mu^+) \sim \text{BR}(H^{++} \rightarrow \tau^+ \tau^+) \approx 1/3$ $\text{BR}(H^+ \rightarrow e^+ \bar{\nu}) \sim \text{BR}(H^+ \rightarrow \mu^+ \bar{\nu}) \sim \text{BR}(H^+ \rightarrow \tau^+ \bar{\nu}) \approx 1/3$

Sensitivity to $H^{++}H^{--} \rightarrow \ell^+\ell^+, \ell^-\ell^-$ Mode: [†]

Nearly background-free.



With 300 fb^{-1} integrated luminosity,
a coverage upto $M_{H^{++}} \sim 1 \text{ TeV}$ even with $BR \sim 40 - 50\%$.

Possible measurements on BR 's.

[†]Pavel Fileviez Perez, Tao Han, Gui-Yu Huang, Tong Li, Kai Wang,
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(5). Type III See-saw at the LHC: T^0 , T^\pm

Lepton flavor combination determines the ν mass pattern: †

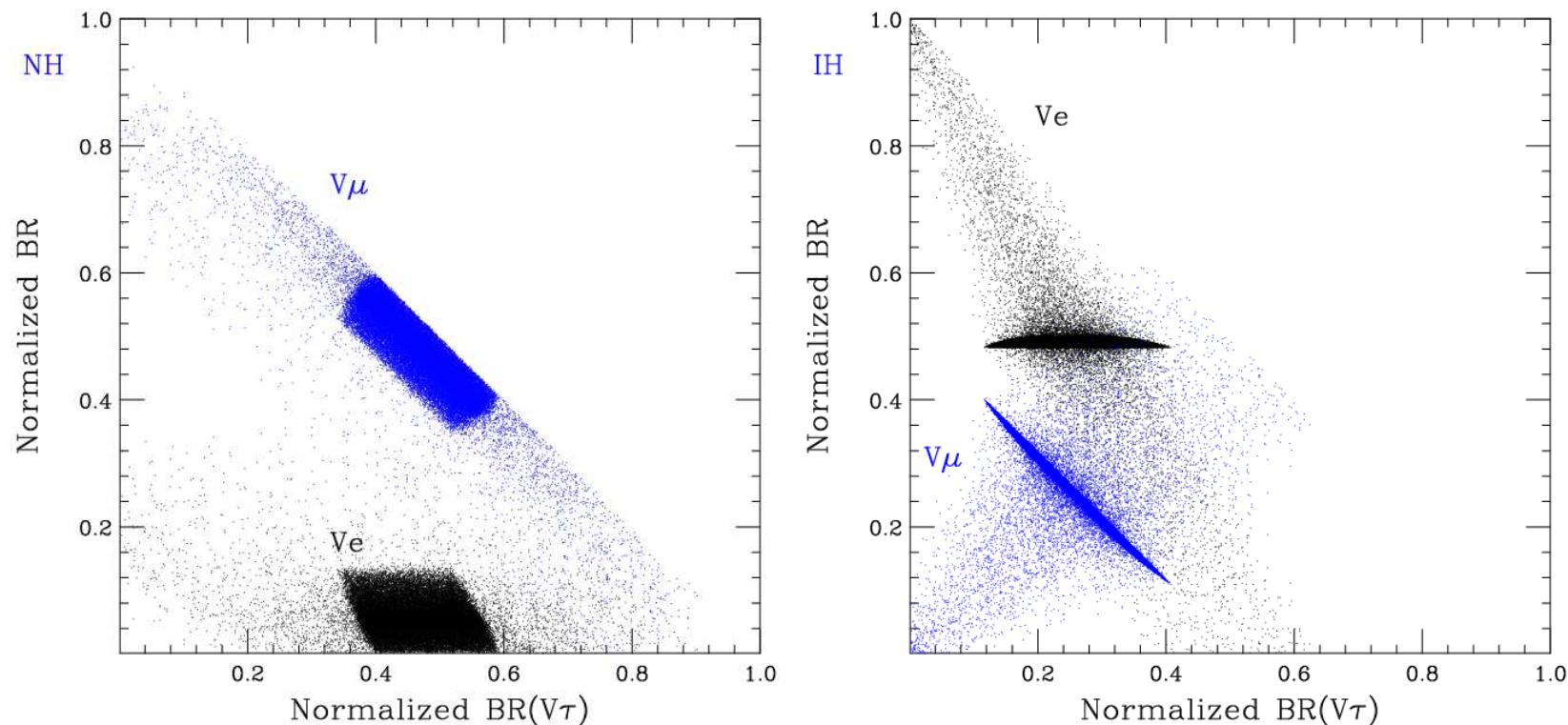
$$m_\nu^{ij} \sim -v^2 \frac{y_T^i y_T^j}{M_T}, \quad BR(T^{\pm,0} \rightarrow W^\pm \ell, Z \ell) \sim y_T^2 \sim V_{PMNS}^2 \frac{M_T m_\nu}{v^2}.$$

† Abdesslam Arhrib, Borut Bajc, Dilip Kumar Ghosh, Tao Han, Gui-Yu Huang, Ivica Puljak, Goran Sejanovic, arXiv:0904.2390.

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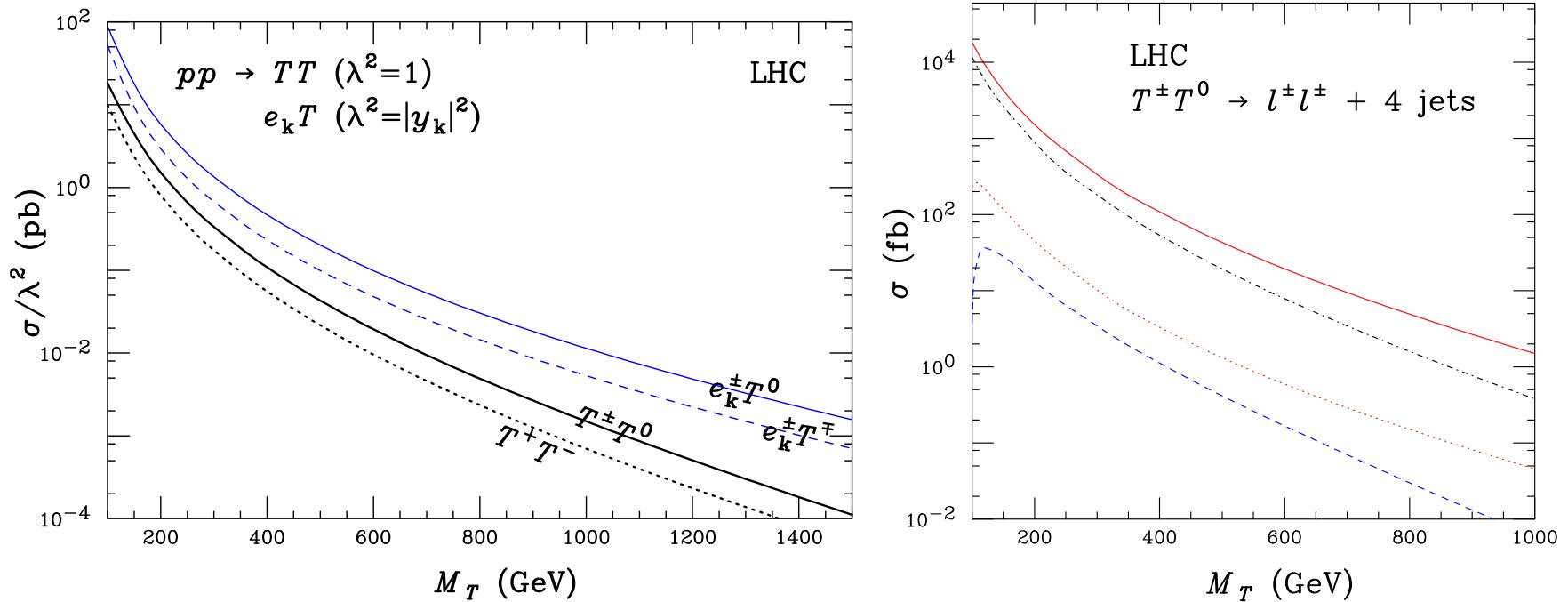
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Production rates at the Tevatron/LHC: \dagger

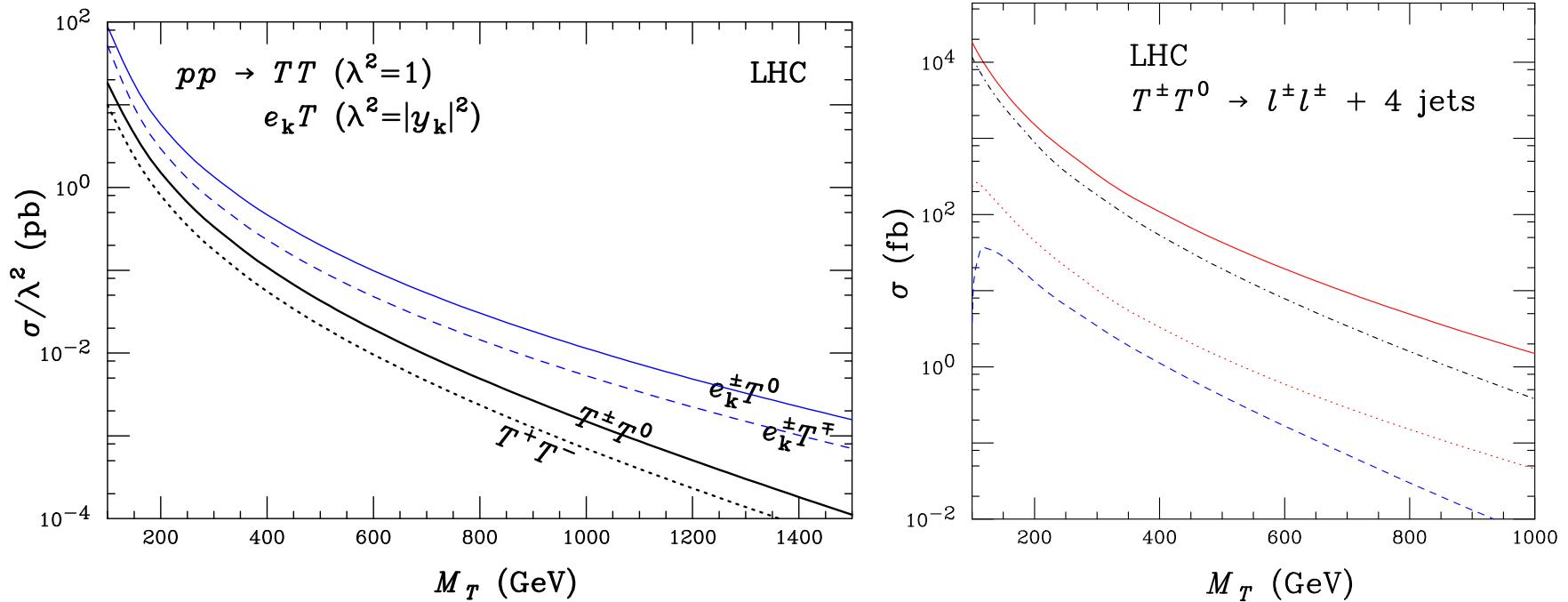


- Single production $T^\pm \ell^\mp$, $T^0 \ell^\pm$:

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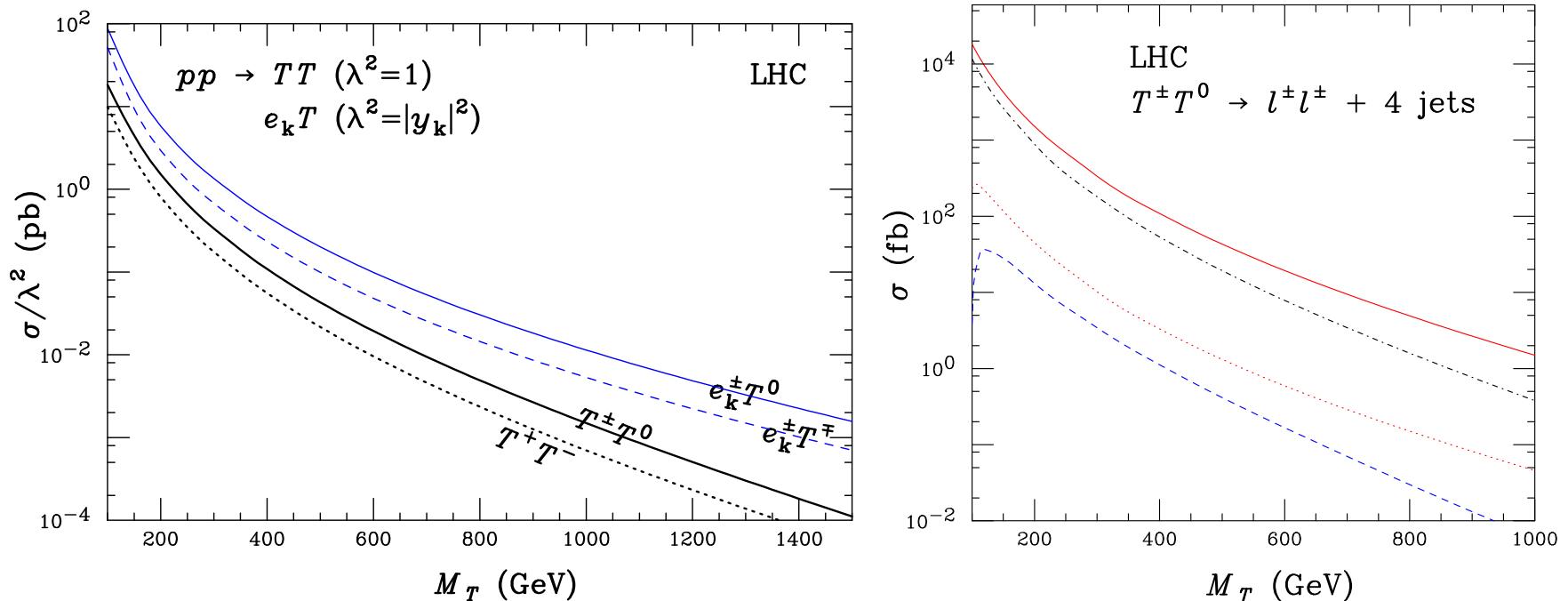
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The See-saw models for m_ν may be the best playground for synergies between the intensity and energy frontiers.
(connecting to the cosmo frontier as well.)